

Subject: Mathematics II

Instructor: Dr. Mohanad Farhan Hamid

References: 1. Thomas' Calculus, 11th edition
2. Stewart Calculus, 8th edition
3. Kreyszig Advanced Engineering Mathematics, 10th edition

Description: The course continues the material the students learnt in their first year. The topics include vectors in 2 and 3-dimensional space, vector-valued functions, partial derivatives, double and triple integrals, infinite series and an introduction to differential equations.

Week no.	Lecture	Topics
1	Space coordinate systems	<ol style="list-style-type: none">1. Points in three-dimensional space2. Vectors in two and three-dimensional space3. Analytic geometry in space
2	Operations on vectors	<ol style="list-style-type: none">1. Addition of vectors (geometrically and algebraically)2. Dot product
3	Cross product	Geometric and algebraic meaning of cross product
4	Equations of lines in space	<ol style="list-style-type: none">1. Parametric equations of a line in space2. Relation between two lines (parallel, intersecting or skew)3. Distance from a point to a line4. Distance between two parallel lines
5	Planes	<ol style="list-style-type: none">1. Equations of planes2. Relation between two planes (parallel or intersecting)3. Distance from a point to a plane4. Distance from a line to a parallel plane5. Distance between two parallel planes
6	Vector-valued functions	<ol style="list-style-type: none">1. Their derivatives and integrals2. (Unit) tangent vector3. Tangent line
7	Quadric surfaces	<ol style="list-style-type: none">1. Recognizing the quadric surface from its equation2. Sketching quadric surfaces
8	Cylinders	Recognizing cylinders that are parallel to one of the coordinate axes and sketching them.

9	Multivariable functions	Functions of two or more variables
10	Partial derivatives	<ol style="list-style-type: none"> 1. The two partial derivatives $\frac{\partial f}{\partial x}$ and $\frac{\partial f}{\partial y}$ 2. Their geometric meanings 3. Computing them
11	Tangent plane and linear approximation	Using partial derivatives to find the tangent plane to a surface and the linear approximation at a point.
12	Chain rule	<ol style="list-style-type: none"> 1. Differentials of x, y and z and total differentials 2. Chain rule
13	Directional derivative	Finding the derivative in the direction of a given vector
14	Gradient	<ol style="list-style-type: none"> 1. Gradient vector 2. Direction of maximum and minimum rate of change
15	Partial derivatives with constrained variables	Finding the partial derivatives of a function if there are some constraints on the variables
16	Double integrals I	Meaning, technique and applications of double integrals over rectangular regions
17	Double integrals II	<ol style="list-style-type: none"> 1. Finding double integrals over non-rectangular regions 2. Reversing the order of the variables 3. Dividing the region of integration
18	Polar coordinates	<ol style="list-style-type: none"> 1. Review of polar coordinates 2. Transforming from cartesian to polar coordinates and vice-versa 3. Sketching curves in polar coordinates
19	Double integrals in polar coordinates I	Finding double integrals in polar coordinates
20	Double integrals in polar coordinates II	Converting double integrals into polar coordinates
21	Triple integrals I	Triple integrals over rectangular boxes
22	Triple integrals II	Reversing the order of a triple integral
23	Triple integrals III	Triple integrals in cylindrical coordinates
24	Infinite series	Definition and examples of infinite series
25	Convergence tests I	<ol style="list-style-type: none"> 1. n-the term test 2. Comparison tests

26	Convergence tests II	<ol style="list-style-type: none"> 1. Limit comparison test 2. Ratio test
27	Convergence tests III	Alternating series: conditional and absolute convergence
28	Differential equations	<ol style="list-style-type: none"> 1. Physical problems stated as differential equations 2. Solutions of differential equations
29	Solution techniques I	<ol style="list-style-type: none"> 1. Separation of variables 2. Linear 1st order differential equations
30	Solution techniques II	<ol style="list-style-type: none"> 1. Bernoulli equations 2. Exact differential equations